# Third Semester B.E. Degree Examination, Dec.09/Jan. 10 Engineering Mathematics - III 

Time: 3 hrs.
Max. Marks:100

## Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

## PART - A

1 a. Obtain Fourier series for the function $f(x)$ given by
$\mathrm{f}(\mathrm{x})=\left\{\begin{array}{lc}1+\frac{2 \mathrm{x}}{\pi}, & -\pi \leq \mathrm{x} \leq 0 \\ 1-\frac{2 \mathrm{x}}{\pi}, & 0 \leq \mathrm{x} \leq \pi\end{array}\right.$
and hence deduce that $\frac{\pi^{2}}{8}=\frac{1}{1^{2}}+\frac{1}{3^{2}}+\frac{1}{5^{2}}+$ $\qquad$ (07 Marks)
b. Find the half-range cosine series for the function $f(x)=(x-1)^{2}$ in the interval $0<x<1$.
(07 Marks)
c. Obtain the constant term and the coefficients of the first sine and cosine terms in the Fourier expansion of $y$ as given in the following table.
(06 Marks)

| x | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | 9 | 18 | 24 | 28 | 26 | 20 | 9 |

2 a. Find the Fourier transform of $f(x)=\left\{\begin{array}{cc}1-x^{2}, & |x| \leq 0 \\ 0, & |x|>\pi\end{array}\right.$.
Hence evaluate $\int_{0}^{\infty} \frac{x \cos x-\sin x}{x^{3}} \cdot \cos \left(\frac{x}{2}\right) d x$
(07 Marks)
b. Find the Fourier cosine transform of $\mathrm{e}^{-\mathrm{x}^{2}}$
(07 Marks)
c. Find the Fouffer sine transform of $\mathrm{e}^{-|x|}$. Hence show that $\int_{0}^{\infty} \frac{\mathrm{x} \sin \mathrm{mx}}{1+\mathrm{x}^{2}} \mathrm{dx}=\frac{\pi}{2} . \mathrm{e}^{-\mathrm{m}}, \mathrm{m}>0$.
(06 Marks)
3 a. Form the partial differential equation by eliminating the arbitrary functions $f$ and $g$ from the relation $z=y^{2}+2 f\left(\frac{1}{x}+\log y\right)$
(07 Marks)
b. Solve $\frac{\partial^{3} t}{\partial x^{2} \partial y}+18 x y^{2}+\sin (2 x-y)=0$
(07 Marks)
c. Solve $(\mathrm{mz}-\mathrm{ny}) \frac{\partial \mathrm{z}}{\partial \mathrm{x}}+(\mathrm{nx}-\mathrm{lz}) \frac{\partial \mathrm{z}}{\partial \mathrm{y}}=(\mathrm{ly}-\mathrm{mx})$
(06 Marks)
4 a. Derive one dimensional heat equation by taking $u(x, t)$ as the temperature, $x$ is the distance and $t$ is the time. (Write the figure also.)
(07 Marks)
b. Obtain the D'Almbert's solution of the wave equation $u_{t t}=C^{2} u_{x x}$, subject to the condition $u(x, o)=f(x)$ and $\frac{\partial u}{\partial t}(x, o)=0$.
(07 Marks)
c. Obtain the various solutions of the Laplace's equation $u_{x x}+u_{y y}=0$, by the method of separation of variables.
(06 Marks)

## PART - B

5 a. Complete the real root of the equation $x \log _{10} x-1.2=0$ by Regula-Falsi method, correct to four decimal places.
(07 Marks)
b. Solve the system of equations using Gauss-Jordan method:

$$
\begin{align*}
2 x+5 y+7 z & =52 \\
2 x+y-z & =0 \\
x+y+z & =9 \tag{07Marks}
\end{align*}
$$

c. Using the power method, find the largest Eigen value and the corresponding Eigen vector of the matrix $\mathrm{A}=\left[\begin{array}{ccc}6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3\end{array}\right]$
(06 Marks)

6 a. The area of a circle (A) corresponding to diameter (D) is given below:
(07 Marks)

| D | 80 | 85 | 90 | 95 | 100 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | 5026 | 5674 | 6362 | 7088 | 7854 |

Find the area corresponding to diameter 105 using an appropriate interpolation formula.
b. Use Newton's divided difference formula to find $f(9)$, given the data,
(07 Marks)

| x | 5 | 7 | 14 | 13 | 17 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{x})$ | 150 | 392 | 1452 | 2366 | 5202 |

c. Evaluate $\int_{4}^{5.2} \log _{\mathrm{e}} \mathrm{x} d \mathrm{dx}$ using Weddle's rule, taking 7ordinates.
(06 Marks)

7 a. Derive Euler's equation in the form

$$
\frac{\partial f}{\partial y}-\frac{d}{d x}\left(\frac{\partial f}{\partial y^{\prime}}\right)=0
$$

(07 Marks)
b. Find the curves on which the functional $\int_{0}^{1}\left[\left(y^{\prime}\right)^{2}+12 x y\right] d x$, with $y(0)=0$ and $y(1)=1$ can be extremised.
(07 Marks)
c. Find the geodesics on a surface given that the arc length on the surface is $S=\int_{x_{1}}^{x_{2}} \sqrt{x\left[1+(y)^{2}\right]} d x$
(06 Marks)

8 a. Find the Z-transforms of the following :
i) $\cosh n \theta$
ii) $(\mathrm{n}+1)^{2}$
(07 Marks)
b. Find the inverse $z$-transform of $\frac{z}{(z-1)(z-2)}$.
(07 Marks)
c. Find the response of the system $y_{n+2}-5 y_{n+1}+6 y_{n}=u$, with $y_{0}=0, y_{1}=1$ and $u_{n}=1$ for $\mathrm{n}=0,1,2,3$, by $z$-transform method.
(06 Marks)

|  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

1 a. Sketch any three types of Bravais lattices.
(06 Marks)
b. Determine the relationship between atomic radius and lattice parameters in cubic systems [simple cubic, BCC and FCC].
(06 Marks)
c. Illustrate the steady-state diffusion.
(08 Marks)
2 a. From the tensile stress-strain behaviour for the brass specimen shown in Fig. Q2(a), determine the following :
i) The modulus of elasticity
ii) The yield strength at a strain offset of 0.002 .
iii) The maximum load that can be sustained by a cylindrical specimen having an original diameter of 12.7 mm .
iv) The change in length of specimen originally 250 mm long which is subjected to a tensile stress of 350 MPa .
(12 Marks)


Fig. Q2(a)
b. When a 3000 kg load is applied to a 10 mm diameter ball in a Brinell test of a steel, an indentation of 3.1 mm is produced. Estimate the tensile strength of the steel.
(04 Marks)
c. A piece of copper originally 300 mm long is pulled in tension with a stress of 270 MPa . If the deformation is entirely elastic, what will be the resultant elongation?
$\left(\mathrm{E}=100 \times 10^{3} \mathrm{MPa}\right)$
(04 Marks)
3 a. Illustrate the stages in the cup and cone facture
(08 Marks)
b. What is fatigue? Draw the SN curves for i) a material that displays a fatigue limit ii) a material that does not display a fatigue limit.
(08 Marks)
c. Explain how fatigue life can be enhanced.
(04 Marks)

4 a. Explain unlimited suitability and limited solubility with examples
(08 Marks)
b. A cooling curve is shown in Fig. Q4(b). Determine the following :
i) The pouring temperature
ii) The solidification temperature
iii) The superheat
iv) The cooling rate, just before solidification beings
v) The total solidification time
vi) The local solidification time.
(06 Marks)


Fig. Q4(b)


Fig. Q4(c)
c.

Calculate the amounts of $\alpha$ and L at $1250^{\circ} \mathrm{C}$ and $175^{\circ} \mathrm{C}$ in the $\mathrm{Cu}-40 \% \mathrm{Ni}$ alloy shown in Fig. Q4(c).
(06 Marks)

## PART-B

5 a. Write the three invariant reactions in the $\mathrm{Fe}-\mathrm{Fe}_{3} \mathrm{C}$ phase diagram.
(06 Marks)
b. What is a plain carbon steel? Discuss the transformation of eutectoid steel $(0.8 \% \mathrm{C})$ with slow cooling.
(08 Marks)
c. Illustrate the effects alloying elements on the eutectoid temperature of steels.
(06 Marks)
a. Illustrate the yariation in the microstructure of eutectoid plain-carbon steel by continuously cooling at differentrates.
(12 Marks)
b. Schematically illustrate the customary quenching and tempering process for a plan-carbon steel.
(08 Marks)

7 a. Discuss AISI-SAE designation of steels, with examples.
(05 Marks)
b. Show schematically, the microstructures of the following cast irons : gray iron, white iron, malleable iron, ductile iron and compacted graphite iron.
(15 Marks)

8 a. What is corrosion? Discuss grain-grain boundary galvanic cells.
(08 Marks)
b. Explain 'Two metal corrosion'.
(06 Marks)
c. Explain how underground pipelines are protected using a magnesium anode.


# Third Semester B.E. Degree Examination, Dec.09/Jan. 10 <br> Basic Thermodynamics 

Time: 3 hrs.
Max. Marks:100

# Note: 1. Answer any FIVE full questions, selecting at least TWO questions from each part. <br> 2. Use of Thermodynamics Charts and Tables is permitted. 

## PART - A

1 a. Distinguish between:
i) Microscopic and macroscopic approaches of thermodynamics
ii) Intensive and extensive properties.
(06 Marks)
b. Explain mechanical, chemical and thermal equilibrium. (06 Marks)
c. State zeroth law of thermodynamics. The emf, in millivolts in a thermocouple with the test junction at $t^{\circ} \mathrm{C}$ on gas thermometer scale and reference junction at ice point is given by $\mathrm{e}=0.0367 \mathrm{t}+1.33 \times 10^{-4} \mathrm{t}^{2}$. The millivolt meter is calibrated at iee point and steam points. What will this thermometer read in a place where the gas thermometer reads $50^{\circ} \mathrm{C}$ ?
(08 Marks)
2 a. Define thermodynamic work and heat.
(04 Marks)
b. Derive an expression for displacement work for polytropic process.
(06 Marks)
c. A cylinder contains one kg of fluid at an initial pressure of 20 bar. The fluid is allowed to expand reversibly behind a piston according to lav $\mathrm{PV}^{2}=\mathrm{C}$ untill the volume is doubled. The fluid is then cooled reversibly at constant pressure untill the piston regains its original position, heat is then supplied reversibly with the piston firmly locked in this position untill the pressure rises to the original value of 20 bar. Calculate the net work done by the fluid for an initial volume of $0.05 \mathrm{~m}^{3}$.
(10 Marks)
3 a. State : i) I law of thermodynamics as applied to a closed system
ii) Two-property rule.
(04Marks)
b. A fluid system undergoes non-flow frictionless process following the pressure - volume relation as $P=\frac{5}{V} 1.5$, where $P$ is in bar and $V$ is in $\mathrm{m}^{3}$. During the process volume changes from $0.15 \mathrm{~m}^{3}$ to $0.05 \mathrm{~m}^{3}$ and the system rejects 45 kJ of heat. Determine: i) Change in internal energy; ii) Change in enthalpy.
(08 Marks)
c. A fluid flows steadily through a rotary device. For a kg of fluid, the heat transfer out of the device is 25 kJ . The fluid properties at the entry are $5 \mathrm{bar}, 50 \mathrm{~m} / \mathrm{s}$ and $0.78 \mathrm{~m}^{3} / \mathrm{kg}$. The corresponding properties at the exit are $1 \mathrm{bar}, 100 \mathrm{~m} / \mathrm{s}$ and $0.97 \mathrm{~m}^{3} / \mathrm{kg}$. The inlet is 5 m above the exit and the internal energy at the entry is greater than that of exit by 119 kJ . Find the out put work.
(08 Marks)
4 a. Represent schematically heat engine, heat pump, and refrigerator. Give their performance.
(06 Marks)
b. Prove that Kelvin Planck and Claussius statements of second law of thermodynamic are equivalent.
(07 Marks)
c. A heat engine is used to drive a heat pump. The heat transfers from the heat engine and the heat pump are used to heat the water circulating through a radiator of a building. If the COP of the heat pump is 4 and the efficiency of the heat engine is 0.3 , how much heat is transferred to the radiator water for every kJ heat transferred to the heat engine? (07 Marks) 1 of 2

## PART - B

5 a. State and prove "Clausius inequality".
(06 Marks)
b. Define entropy and prove that it is a property of the system.
(06 Marks)
c. Obtain an expression for entropy change of a closed system when it undergoes a polytropic process.
(08 Marks)
6 a. Define :
i) Available energy
ii) Availability
iii) Effectiveness.
(06 Marks)
b. Obtain an equation for maximum work available in a non - flow system.
(06 Marks)
c. A system at 500 K receives $7200 \mathrm{~kJ} / \mathrm{min}$ from a source at 1000 K . The temperature of atmosphere is 300 K . Assuming that the temperatures of system and source remain constant during heat transfer, find out
i) The entropy produced during heat transfer.
ii) The decrease in available energy after heat transfer.
(08 Marks)
7 a. Write a neat P - T diagram for a pure substance and define : i) Tripple point ; ii) Critical point.
(06 Marks)
b. Define :
i) Sensible heat of water
ii) Latent heat and
iii) Dryness fraction.
(06 Marks)
c. The following data were obtained in a est on a combined separating and throttling calorimeter.
Pressure of steam sample $=15$ bar
Pressure of steam at exit $=1$ bar
Temperature of steam at exith $=150^{\circ} \mathrm{C}$
Discharge from separating calorimeter $=0.5 \mathrm{~kg} / \mathrm{min}$
Discharge from throtting calorimeter $=10 \mathrm{~kg} / \mathrm{min}$. Determine the dryness fraction of the sample of steam.
(08 Marks)
8 a. Write a short note on Vander Wall's equation.
(05 Marks)
b. Explain reduced properties and compressibility chart.
(05 Marks)
c. A vessel of capacity $3 \mathrm{~m}^{3}$ contains 1 kg mole of $\mathrm{N}_{2} \mathrm{At} 90^{\circ} \mathrm{C}$
i) Calculate pressure and specific volume of gas
ii) If the ratio of specific heats are 1.4 , obtain cp and cv
iii) Subsequently, the gas cools to the atmospheric temperature of $20^{\circ} \mathrm{C}$; evaluate the final pressure of gas.
iv) Evaluate the increase in specific internal energy, the increase in specific enthalpy, increase in specific entropy and heat transfer.
(10 Marks)


# Third Semester B.E. Degree Examination, Dec.09-Jan. 10 Mechanics of Materials 

Time: 3 hrs .
Max. Marks:100
Note: Answer any FIVE full questions, selecting atleast TWO questions from each Part.

## PART - A

1 a. Define i) stress ii) principle of super position.
(04 Marks)
b. A member $A B C D$ is subjected to point loads as shown in fig.Q1(b), calculate i) Force $P$ necessary for equilibrium ii) Total elongation of the bar. Take $\mathrm{E}=210 \mathrm{GN} / \mathrm{m}^{2}$.

(06 Marks)
Fig.Q1(b)
c. Two vertical rods one of steel and the other of copper are each rigidly fixed at the top and 500 mm apart. Diameters and lengths of each rod are 20 mm and 4 m respectively. A cross bar fixed to the rods at the lower ends carries a load of 5 kN , such that the cross bar remains horizontal even after loading. Find the stress im each rod and the position of the load on the bar. Take $E_{s}=2 \times 10^{5} \mathrm{~N} / \mathrm{mm}^{2}$ and $E_{c}=1 \times 10^{5} \mathrm{~N} / \mathrm{mm}$.
(10 Marks)
2 a. Define Bulk modulus. Derive an expression for Young's modulus in terms of bulk modulus and Poisson's ratio.
(08 Marks)
b. i) Define Thermal stress.
(02 Marks)
ii) Calculate the values of the stress and strain in portion AC and CB of the steel bar shown in Fig Q2b (ii). A close fit exists at both the rigid supports at room temperature and the temperature is raised by $75^{\circ} \mathrm{C}$, Take $\mathrm{E}=200 \mathrm{GPa}$ and $\alpha=12 \times 10^{-6}$ per ${ }^{0} \mathrm{C}$ for steel. Area of cross - sections of AC is $400 \mathrm{~mm}^{2}$ and of $B C$ is $800 \mathrm{~mm}^{2}$.
(10 Marks)


Fig.Q2b(ii)
3 a. Define i) principal stress
ii) principal strain.
(04 Marks)
b. A machine component is subjected to the stresses as shown in Fig. Q3(b). Find the normal and shearing stresses on the section AB inclined at an angle of $60^{\circ}$ with $\mathrm{x}-\mathrm{x}$ axis. Also find the resultant stress on the section. Verify the above results by drawing Mohr's circle.

(16 Marks)
Fig.Q3(b)
1 of 2

4 a. Derive an expression for circumferential stress and longitudinal stress for a thin shell subjected to an internal pressure.
(06 Marks)
b. Derive an expression for the radial pressure and hoop stress for a thick spherical shell.
(06 Marks)
c. A thick spherical shell of 200 mm internal diameter is subjected to an internal fluid pressure of $7 \mathrm{~N} / \mathrm{mm}^{2}$. If the permissible tensile stress in the shell material is $8 \mathrm{~N} / \mathrm{mm}^{2}$, find the thickness of the shell.
(08 Marks)

## PART - B

5 Draw the bending moment and shear force diagrams for the beam loaded as shown in fig. Q5.
(20 Marks)


Fig.Q5
6 a. Prove the relations $\frac{M}{I}=\frac{\sigma}{Y}=\frac{E}{R}$ with usual notations.
(10 Marks)
b. A T - shaped cross - section of a beam in ig. Qo(b) is subjected to a vertical shear force of 100 kN . Calculate the shear stress at themeural axis and at the junction of the web and the flange. M.I. about the horizontal nentral axis is $0.0001134 \mathrm{~m}^{4}$.
(10 Marks)


7 A beam fength 6 m is simply supported at its ends and carries two point loads of 40 kN at a distance of 1 ma 3 m respectively from the left support. By using Macaulay's method, determine : a) deflection under each load b) maximum deflection c) the point at which maximum deffection occurs. Given $\mathrm{E}=2 \times 10^{5} \mathrm{~N} / \mathrm{mm}^{2}$ and $\mathrm{I}=85 \times 10^{6} \mathrm{~mm}^{4}$.
(20 Marks)
8 a. Two shafts of the same material and of same lengths are subjected to the same torque, if the first shaft is of a solid circular section and the second shaft is of hollow circular section, whose internal diameter is $2 / 3$ of the outside diameter and the maximum shear stress developed in each shaft is the same, compare the weights of the shafts.
(10 Marks)
b. A 1.5 m long column has a circular cross section of 50 mm diameter. One of the ends of the column is fixed in direction and position and other end is free. Take factor of safety as 3 , calculate the safe load using :
i) Rankine's formula, take yield stress $=560 \mathrm{~N} / \mathrm{mm}^{2}$ and $\mathrm{a}=\frac{1}{1600}$ for pinned ends.
ii) Euler's formula, Young's modulus for C.I. $=1.2 \times 10^{5} \mathrm{~N} / \mathrm{mm}^{2}$.
(10 Marks)


# Third Semester B.E. Degree Examination, Dec.09/Jan. 10 Manufacturing Process - I 

Time: 3 hrs.
Max. Marks:100

## Note: Answer any FIVE full questions, selecting <br> at least TWO questions from each part.

## PART - A

1 a. What do you understand by the term 'manufacturing'? Discuss the factors to be considered in the selection of a process for production.
(05 Marks)
b. Define the casting process. Discuss the advantages and disadvantages of the casting process.
(05 Marks)
c. List the different allowances given on a pattern. Sketch and explain the loose piece pattern.
(05 Marks)
d. Write a note on binders and additives, used in moulding.
(05 Marks)
2 a. What are the desirable properties of a moulding sand?
(05 Marks)
b. What is meant by a core? Sketch and explain a balanced cor
(05 Marks)
c. Draw a neat sketch of a gating system showing all the elements;
(05 Marks)
d. Explain with a sketch, the working of jolt type moulding machine.
(05 Marks)
3 a. With neat sketches, briefly explain the different steps involved in shell moulding process and mention its advantages.
(10 Marks)
b. With a neat sketch, explain continuous casting process and mention its advantages.( 10 Marks)

4 a. Explain the construction and working principle of a Cupola furnace, with a sketch. (12 Marks)
b. Explain with a sketch, working of a direct arc electric furnace.
(08 Marks)

## PART - B

5 a. Define welding process. What are the advantages of welding over other manufacturing processes? List the industrial applications of welding.
(08 Marks)
b. Explain the following welding processes with necessary sketches and their field of applications. i) Tungsten inert gas welding (TIG) ii) Atomic hydrogen welding (AHW).
(12 Marks)
6 a. With neat sketches, explain:
i) Seam welding
ii) Projection welding
(12 Marks)
b. With a sketch, explain the electron beam welding. Mention its applications.
(08 Marks)
7 a. Discuss the need for the following, in welding:
i) Flux
ii) Filler material
iii) Electrodes.
(06 Marks)
b. Explain the different welding defects, their causes and remedies.
( $\mathbf{1 0}$ Marks)
c. Write a note on residual stresses, in welding.
(04 Marks)
8 a. Explain soldering and brazing, with examples. Mention their advantages and disadvantages.
(08 Marks)
b. Explain the following, with neat sketches:
i) X-ray radiography
ii) Optical holography.
(12 Marks)
$\square$

## Third Semester B.E. Degree Examination, Dec.08/Jan. 09 <br> (ME/IP/AU/IM/MA/AE/MI) <br> COMPUTER AIDED MACHINE DRAWING

Time: $\mathbf{3}$ hrs.
Max. Marks: 100
Note: 1. Answer any ONE question from each of the parts A, B and C.
2. Use FIRST ANGLE projections only.
3. Missing data if any may suitably be assumed.
4. All the calculations should be on answer sheet supplied.
5. All the dimensions are in mm .
6. Drawing instruments may or may not be used for sketching
7. Part C Assembled View should be in 3D and other 2 views in 2D.
PART - A

1. A hexagonal pyramid sides of base 30 mm and altitude 70 mm is rests with its with its base on the HP and with a side of base parallel to the VP. It is cut by a cutting plane inclined at $35^{0}$ to the HP and perpendicular to the VP and is bisecting the axis. Draw the front view, the sectional view looking from the top and true shape of section.
2. Draw two views of hexagonal headed bolt with nut for a 30 mm diameter bolt. Take length of bolt equal to 125 mm .
(20 marks)
PART - B
3. Draw the top view and sectional front view of single riveted butt joint with double cover plates. The thickness of plate is 14 mm . Show at least three rivets. Indicate all the dimensions. Use snap head rivets and show all calculation on the answer sheet.
(20 marks)
4. Draw bushed-pin type of flexible coupling to connect two shafts of 20 mm diameter for the following views:
(a) Front view with top half in section.
(b) Side view from pin-head end.
(20 marks)

## PART - C

5. Figure 1. shows the details of Screw Jack. Assemble the parts and draw the following views: (i) Front View showing right half in section and (ii) Top View
(60 marks)
6. Figure 2. shows the details of a Tool Head of a Shaper. Assemble the parts and draw
(i) Sectional Front View.
(ii) Top View.



$\square$ MATDIP301

Third Semester BE Degree Examination, Dec.09-Jan. 10 Advanced Mathematics - I

Time: 3 hrs .
Max. Marks:100

## Note: Answer any FIVE full questions.

1 a. Find the modulus and amplitude of $\frac{4+2 i}{2-3 i}$.
(06 Marks)
b. Express the complex number $2+3 \mathrm{i}+\frac{1}{1-\mathrm{i}}$ in the form of $\mathrm{a}+\mathrm{ib}$.
c. Express the complex number $\sqrt{3}+\mathrm{i}$ in the polar form.
(07 Marks)
(07 Marks)

2 a. Find the $\mathrm{n}^{\text {th }}$ derivative of $\mathrm{e}^{-\mathrm{x}} \sin ^{2} \mathrm{x}$.
(06 Marks)
b. Find the $n^{\text {th }}$ derivative of $\frac{x}{(x-1)(2 x+3)}+e^{2 x}$.
c. If $y=\sin ^{-1} x$ then prove that $\left(1+x^{2}\right) y_{n+2}-(2 n+1) x y_{n+1}-n^{2} y_{n}=0$.

3 a. Using Maclaurin's series expand tanx unto the term containing $x^{3}$.
(06 Marks)
b. Find the angle between the radius vector and angent to the curve $\mathrm{r}=\sin \theta+\cos \theta$. ( 07 Marks)
c. With usual notations prove that
i) $\mathrm{P}=\mathrm{r} \sin \phi$
ii) $\frac{1}{\mathrm{p}^{2}}=\frac{1}{\mathrm{p}^{2}}+\frac{1}{\mathrm{p}^{4}}\left(\frac{\mathrm{dt}}{\mathrm{d} \theta}\right)^{2}$.
(07 Marks)

4 a. If $u=f\left(r, s, t\right.$ where $r=\frac{x}{y}, s=\frac{y}{z}, t=\frac{z}{x}$ then prove that $x \frac{\partial u}{\partial x}+y \frac{\partial u}{\partial y}+z \frac{\partial u}{\partial z}=0$.
(06 Marks)
b. If $u=f(x+a y)+g(x-a y)$ then show that $\frac{\partial^{2} u}{\partial y^{2}}=a^{2} \frac{\partial^{2} u}{\partial x^{2}}$.
(07 Marks)
c. If $u=x^{2}-2 y, v=x+y+z, w=x-2 y+3 z$ then find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$.
(07 Marks)

5 a. Obtain the reduction formula for $\int \cos ^{n} \mathrm{xdx}$ where n is a positive integer.
(06 Marks)
b. Evaluate $\int_{0}^{1} x^{6} \sqrt{1-x^{2}} d x$.
(07 Marks)
c. Evaluate $\int_{0}^{1} \int_{x}^{\sqrt{x}}\left(x^{2}+y^{2}\right) d y d x$. .

6 a. Evaluate $\int_{0}^{1} \int_{0}^{2} \int_{1}^{2} x^{2} y z d z d y d x$.
b. Prove that $\sqrt{\frac{1}{2}}=\sqrt{\pi}$.
(07 Marks)
c. Show that $\int_{0}^{\pi / 2} \sqrt{\operatorname{Sin} \theta} \mathrm{~d} \theta \times \int_{0}^{\pi / 2} \frac{\mathrm{~d} \theta}{\sqrt{\operatorname{Sin} \theta}}=\pi$.
(07 Marks)

7 a. Solve $\left(e^{y}+1\right) \operatorname{Cos} x d x+e^{y} \operatorname{Sin} x d y=0$.
(06 Marks)
b. Solve $y d x-x d y=\sqrt{x^{2}+y^{2}} d x$.
(07 Marks)
c. Solve $x \frac{d y}{d x}+y=x^{3} y^{6}$.
(07 Marks)

8 a. Solve $4 \frac{d^{3} y}{d x^{3}}+4 \frac{d^{2} y}{d x^{2}}+\frac{d y}{d x}=0$.
(06 Marks)
b. Solve $\frac{d^{2} x}{d t^{2}}+2 \frac{d x}{d t}+3 x=\operatorname{Sin} t+e^{-t}$.
(07 Marks)
c. Solve $\frac{d^{2} y}{d x^{2}}-2 \frac{d y}{d x}+y=x e^{x} \sin x$.
(07 Marks)

